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# Improving the Interpretation of Fixed Effects Regression Results\*

JONATHAN MUMMOLO AND ERIK PETERSON

For example, it is well known that with panel data, fixed effects models eliminate time-invariant confounding, estimating an independent variable's effect using only within-unit variation. When researchers interpret the results of fixed effects models, they should therefore consider hypothetical changes in the independent variable (counterfactuals) that could plausibly occur within units to avoid overstating the substantive importance of the variable's effect. In this article, we replicate several recent studies which used fixed effects estimators to show how descriptions of the substantive significance of results can be improved by precisely characterizing the variation being studied and presenting plausible counterfactuals. We provide a checklist for the interpretation of fixed effects regression results to help avoid these interpretative pitfalls.

The fixed effects regression model is commonly used to reduce selection bias in the estimation of causal effects in observational data by eliminating large portions of variation thought to contain confounding factors. For example, when units in a panel data set are thought to differ systematically from one another in unobserved ways that affect the outcome of interest, unit fixed effects are often used since they eliminate all between-unit variation, producing an estimate of a variable's average effect within units over time (Allison 2009; Wooldridge 2010). Despite this feature, social scientists often fail to acknowledge the large reduction in variation imposed by fixed effects. This article discusses two important implications of this omission: imprecision in descriptions of the variation being studied and the use of implausible counterfactuals—discussions of the effect of shifts in an independent variable that are rarely or never observed within units—to characterize substantive effects.

By using fixed effects, researchers make not only a methodological choice but a substantive one (Bell and Jones 2015), narrowing the analysis to particular dimensions of the data, such as within-country (i.e., over time) variation. By prioritizing within-unit variation, researchers forgo the opportunity to explain between-unit variation since it is rarely the case that between-unit variation will yield plausible estimates of a causal effect. When using fixed effects, researchers should emphasize the variation that is being used in descriptions of their results. Identifying which units actually vary over time (in the case of unit fixed effects) is also crucial for gauging the generalizability of results, since units without variation provide no information during one-way unit-fixed effects estimation (Plümper and Troeger 2007).<sup>1</sup>

In addition, because the within-unit variation is always smaller (or at least, no larger) than the overall variation in the independent variable, researchers should use within-unit variation to motivate counterfactuals when discussing the substantive impact of a treatment. For example, if

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<sup>&</sup>lt;sup>1</sup> The same is true for time periods which contain no variation in the treatment when time dummies are used.

#### 2 MUMMOLO AND PETERSON

only within-country variation in some treatment X is used to estimate a causal effect, researchers should avoid discussing the effect of changes in X that are larger than any changes observed within units in the data. Besides being unlikely to ever occur in the real world, such "extreme counterfactuals," which extrapolate to regions of sparse (or nonexistent) data rest on strong modeling assumptions, and can produce severely biased estimates of a variable's effect if those assumptions fail (King and Zeng 2006).

In what follows, we replicate several recently published articles in top social science journals that used fixed effects. Our intention is not to cast doubt on the general conclusions of these studies, but merely to demonstrate how adequately acknowledging the variance reduction imposed by fixed effects—and formulating plausible counterfactuals after estimation that account for this reduction—can improve descriptions of the substantive significance of results.<sup>2</sup> We conclude with a checklist to help researchers improve discussion of fixed effects results.

#### VARIANCE REDUCTION WITH FIXED EFFECTS

Consider the standard fixed effects dummy variable model:

$$Y_{it} = \alpha_i + \beta X_{it} + \varepsilon_{it}, \tag{1}$$

in which an outcome Y and an independent variable (treatment) X are observed for each unit *i* (e.g., countries) over multiple time periods *t* (e.g., years), and a mutually exclusive intercept shift,  $\alpha$ , is estimated for each unit *i* to capture the distinctive, time-invariant features of each unit. This results in an estimate of  $\beta$  that is purged of the influence of between-unit time-invariant confounders.<sup>3</sup>

While the overall variation in the independent variable may be large, the within-unit variation used to estimate  $\beta$  may be much smaller. The same is true when dummies for time are included (i.e., year dummies), in which case  $\beta$  is estimated using only within-year variation in the treatment. When multi-way fixed effects are employed (e.g., country *and* year dummies, as in a generalized difference-in-differences estimator),<sup>4</sup> the variance reduction is even more severe.

#### PUBLISHED EXAMPLES

To evaluate how often researchers acknowledge the variance reduction imposed by fixed effects when interpreting results, we conducted a literature review of empirical studies published in the *American Political Science Review* or the *American Journal of Political Science*, which used linear fixed effects estimators between 2008 and 2015.<sup>5</sup> Of the 54 studies we identified fitting these

$$(Y_{it} - \overline{Y_i}) = \beta (X_{it} - \overline{X_i}) + (\varepsilon_{it} - \overline{\varepsilon_i}).$$
<sup>(2)</sup>

Equation 2 makes plain that  $\beta$  is estimated solely based on deviations from each unit's average treatment value over time.

<sup>4</sup> Recent scholarship (Kim and Imai, n.d.) has highlighted assumptions that often get overlooked during fixed effects estimation which can bias causal estimates. In the present analysis, we take the research designs in the published work we examine as given to focus solely on the issues associated with variance reduction.

<sup>&</sup>lt;sup>2</sup> Our critiques also have no bearing on the statistical significance of any published results.

<sup>&</sup>lt;sup>3</sup> In this scenario, between-unit variation is eliminated by demeaning the data within units (e.g., countries) during estimation (see e.g., Greene 2008, 198; Baltagi 2005; Cameron and Trivedi 2005, 726). That is, we could recover an identical estimate of  $\beta$  by omitting unit dummy variables and estimating the following:

<sup>&</sup>lt;sup>5</sup> Given our interest is in how researchers formulate counterfactuals, we excluded articles which featured a dichotomous treatment, since there is little discretion for counterfactuals in the case of a 0/1 treatment (i.e., the treatment either occurs or it does not). See Appendix for full details on the parameters of this literature review.

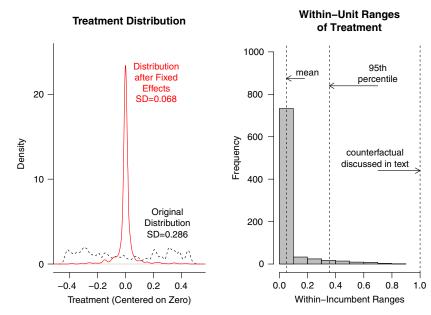


Fig. 1. The left panel displays the distribution of the treatment, media congruence, from Snyder and Strömberg (2010) before and after the incumbent and year fixed effects used in that study are applied Note: Both distributions were centered on 0 before plotting to ease comparisons of their spread. The right panel shows the within-incumbent ranges of the treatment. While the right panel does not perfectly capture the relevant variation since it does not account for two-way fixed effects, we include it here to help motivate within-unit counterfactuals.

parameters, roughly 69 percent of studies explicitly described the variation being used during estimation (e.g., "... we include a full set of industry-year fixed effects ... so that comparisons are within industry-year cells" (Earle and Gehlbach 2015, 713)). Only one study, Nepal, Bohara and Gawande (2011), explicitly quantified the size of typical shifts in levels of the treatment within units, allowing readers to judge the plausibility of the counterfactuals being discussed.<sup>6</sup>

Attention to this variance reduction has the potential to greatly influence how researchers characterize the substantive significance of results (i.e., whether a treatment imposes an effect large enough to induce a politically meaningful change in the outcome). For example, Figure 1 shows the distribution of the treatment in Snyder and Strömberg (2010) before and after fixed effects are applied.<sup>7</sup> This study estimates the effects of media market congruence (the alignment between print media markets and US congressional incumbents, a continuous variable takes values between 0 and 1), on both the public and political elites. As the left panel of the plot shows, the distribution of congruence is fairly uniform across congressional incumbents and years in the pooled sample. However, once year and incumbent fixed effects are applied, the amount of variation is drastically reduced (the standard deviation of the variable drops from 0.286 to 0.068, a reduction of 76 percent). The reason is that much of the variation in these data is between incumbents, all of which is discarded by the inclusion of incumbent dummies in several models in this study. The right panel of the figure shows the distribution of within-incumbent ranges of the treatment. As the histogram shows, the mean range observed within incumbents is roughly 0.05,

<sup>&</sup>lt;sup>6</sup> The study supplied within-district standard deviations in table 1.

<sup>&</sup>lt;sup>7</sup> Specifically, we residualize the treatment with respect to year and incumbent dummies (Lovell 1963).

	(1)	(2)	(3)	(4)	(5)
Studies	β	$\widehat{\mathbf{SD}}(x)$	$\widehat{\mathbf{SD}}(\tilde{x})$	Δ% (3) versus (2)	$\frac{\text{Stated Counterfactual}}{\widehat{\text{SD}}(\tilde{x})}$
Berrebi and Klor (2008)	0.004	1.052	0.839	-20.284	1.192
Gasper and Reeves (2011)	2.65	0.445	0.365	-17.89	2.736
Ichino and Nathan (2013)	0.316	0.219	0.082	-62.512	2.667
Scheve and Stasavage (2012)	23.017	0.159	0.112	-29.563	8.953
Snyder and Strömberg (2010)	0.279	0.286	0.068	-76.33	14.768

 TABLE 1
 Replication Results from Recent Studies Using Fixed Effects

*Note:* Column 1 displays the estimated unstandardized regression coefficient of interest in each study. Columns 2 and 3 display the standard deviations of the key independent variable before and after residualizing with respect to fixed effects, respectively. Column 4 displays the percent difference between these two SDs. Column 5 displays the ratio of the counterfactual change in the treatment discussed in the article versus our preferred counterfactual, the revised standard deviation of *X*. See Appendix for details on the referenced published counterfactuals.

and is about 0.36 at the 95th percentile of the distribution of ranges. Roughly 44 percent of the time, the treatment does not vary at all within unit. Noting this fact would help to inform the generalizability of the result.

While Snyder and Strömberg (2010) acknowledge the use of a within-unit estimator,<sup>8</sup> the authors go on to consider a 0-to-1 shift in the treatment when discussing its impact on the probability that an individual recalls the name of their member of Congress. The paper states that, "... a change from the lowest to the highest values of congruence is associated with a 28 percent increase in the probability of correctly recalling a candidate's name. This is about as large as the effect of changing a respondent's education from grade school to some college" (Snyder and Strömberg 2010, 372). A 0-to-1 shift is beyond the observed range even in the original data (i.e., before the fixed effects adjustment). When a more realistic counterfactual is used—the standard deviation of the treatment after residualizing with respect to the incumbent and year dummies the authors employ—a more modest effect of a 1.9 percentage point increase in the probability of recalling a representative's name is recovered. A shift the size of the 95th percentile of within-incumbent ranges produces a 9.9 percentage point effect. Apart from rare cases in which very large shifts in congruence occur within units over time, the results suggest that the treatment exerts only a small effect on representative name recall.

In another example, Ichino and Nathan (2013) discuss the effect of changing the level of an ethnic group surrounding a polling station, stating that, "... a one standard deviation increase in the spatially weighted population share of Akans beyond a polling station (about 0.21) results in a predicted 6.9 percentage point greater NPP presidential vote share" (Ichino and Nathan 2013, 351–2). This counterfactual is based on the standard deviation of the overall distribution of the independent variable. However, the fixed effects estimator employed in this analysis only uses the within-parliamentary constituency distribution, and a 1-SD shift in this revised distribution produces a 2.6 percentage point effect, a decrease of 63 percent compared with the reported effect.

Table 1 displays results from replications of five published studies.<sup>9</sup> In each case, we generated the revised version of the independent variable after residualizing with respect to the included fixed effects (we label this residualized variable  $\tilde{x}$ ), in order to assess the consequences

<sup>&</sup>lt;sup>8</sup> Snyder and Strömberg (2010) states that the estimation strategy, "... focuses on variation within congressional districts," (357).

<sup>&</sup>lt;sup>9</sup> These studies were chosen based on the availability of functional replication files and also to represent different substantive fields in political science.

of variance reduction. As the results show, considering a 1 SD shift in  $\tilde{x}$ , as opposed to a 1-SD shift in the original distribution, reduces estimated treatment effects by as much as 76 percent (column 4). Column 5 compares the counterfactual shifts in X discussed in each article to  $\widehat{SD}(\tilde{x})$ . In the case of Berrebi and Klor (2008), the discussed counterfactual is quite plausible (i.e., the ratio is close to 1), while the counterfactuals discussed in Gasper and Reeves (2011) and Ichino and Nathan (2013) are close to three times the size of the revised standard deviation. The changes in X discussed in Scheve and Stasavage (2012) and Snyder and Strömberg (2010) —both shifts from the minimum to the maximum of the independent variable's range—are roughly 9 and 15 times the size of a typical shift in the revised distribution in X, respectively, indicating that changes this large are rarely observed in the data.<sup>10</sup>

Since most political science studies using fixed effects seek to characterize on-average effects rather than effects within any particular unit, we consider the within-unit standard deviation a sensible counterfactual to consider since it represents the average amount the independent variable deviates from the mean after fixed effects are employed. Still, some might wish to convey treatment effects in the common scenario of a one-unit shift. This may be especially useful if the treatment being studied is dichotomous or a count variable that takes only integer values, in which case unit shifts arguably make more substantive sense to consider (this is the case with Berrebi and Klor (2008) and Gasper and Reeves (2011), for example). Here too, variance reduction should be noted, since in some cases even a one-unit shift can represent a change that is several times the size of a typical shift within units. Researchers are of course free to discuss such counterfactuals, but we recommend discussing the magnitude of the hypothetical change in X relative to the variation being used during estimation (i.e., the ratio displayed in column 5) so readers have a sense of whether the hypothetical change in X is rare.

#### CONCLUSION

Because it reduces concerns that omitted variables drive any associations between dependent and independent variables, many researchers use linear fixed effects regression. This estimator reduces the variance in the independent variable and narrows the scope of a study to a subset of the overall variation in the data set. While some researchers readily acknowledge these features, many studies can benefit from more specificity in the description of the variation being studied and the consideration of counterfactuals that are plausible given the variation being used for estimation (e.g., a typical within-unit shift in X).

### CHECKLIST FOR INTERPRETING FIXED EFFECTS RESULTS

When researchers employ linear fixed effects models, we recommend<sup>11</sup> the following method for evaluating results after estimation:

1. Isolate relevant variation in the treatment: Residualize the key independent variable with respect to the fixed effects being employed (Lovell 1963). That is, regress the treatment on the dummy variables which comprise the fixed effects and store the resulting vector of residuals. This vector represents the variation in X that is used to estimate the coefficient of interest in the fixed effects model.<sup>12</sup>

<sup>&</sup>lt;sup>10</sup> Note that several articles discussed more than one counterfactual scenario. We highlight one from each article here for clarity of discussion.

<sup>&</sup>lt;sup>11</sup> See Appendix for R code to apply these recommendations.

<sup>&</sup>lt;sup>12</sup> This approach is often preferable to manually demeaning the data since it easily accommodates multi-way fixed effects.

#### 6 MUMMOLO AND PETERSON

- 2. Identify a plausible counterfactual shift in X given the data: Generate a histogram (as in Figure 1) of the within-unit ranges of the treatment to get a sense of the relevant shifts in X that occur in the data. Compute the standard deviation of the transformed (residualized) independent variable, which can be thought of as a typical shift in the portion of the independent variable that is being used during the fixed effects estimation. Multiply the estimated coefficient of interest by the revised standard deviation of the independent variable to assess substantive importance. Note for readers what share of observations do not exhibit any variation within units to help characterize the generalizability of the result. Alternatively, if describing the effect of a one-unit shift, or any other quantity, note the ratio of this shift in X to the within-unit standard deviation, as well as its location on the recommended histogram, to gauge how typically a shift of this size occurs within units.
- 3. Clarify the variation being studied: In describing the scope of the research and in discussing results after fixed effects estimation, researchers should clarify which variation is being used to estimate the coefficient of interest. For example, if only within-unit variation is being used, then phrases like "as *X* changes within countries over time, *Y* changes …" should be used when describing treatment effects.
- 4. Consider the outcome scale: Consider characterizing this new effect in terms of both the outcome's units and in terms of standard deviations of the original and transformed outcome (i.e., the outcome residualized with respect to fixed effects). The substance of particular studies should be used to guide which outcome scale is most relevant.

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# Appendix

## Parameters of Literature Review

We searched every issue of the APSR and AJPS on Google Scholar between 2008 and 2015 for the term "fixed effects," which returned roughly 290 articles. We trimmed this sample to include only observational studies (no randomized experiments, in which fixed effects are used merely for efficiency gains and are orthogonal to treatment assignment by design) that used the term "fixed effects" in the traditional econometric sense, i.e. mutually exclusive and exhaustive group indicators such as units, time periods, regions, etc., (as opposed to a nonvarying coefficient in a hierarchical model). We retained studies which used fixed effects in a core analysis of a central hypothesis based on our reading of the manuscript (e.g. not simply in a footnoted robustness check). We also excluded methods, theoretical and review articles and all articles that did not use plain ordinary least squares regression. Given our interest is in how researchers formulate counterfactuals, we also excluded articles which featured a dichotomous treatment, since there is little discretion for counterfactuals in the case of a 0/1 treatment (i.e. the treatment either occurs or it does not). The end result was a sample of 55 articles. We then read the sections of each study outlining the research design and empirical results and coded each study for whether (1) the article explicitly discussed the variation being used during estimation (i.e. "within countries over time"...); (2) the article discussed a counterfactual when discussing results; and (3) the counterfactual shift that was considered in X was chosen based on the transformed distribution of X (e.g. the within-unit distribution in the case of unit fixed effects). We counted articles which explicitly mentioned the within-unit variation being used, or that described fixed effects as "controlling for between-unit differences," as satisfying the first criteria, which we regard as lenient. While we cannot guarantee that we did not miss a relevant case, we think this sample provides a good portrait of the use and interpretation of fixed effects estimators in the top tier of the field today.

### Counterfactuals from Published Examples

Below are the counterfactuals discussed in the published examples we highlight in Table 1. Note that it is not uncommon for several counterfactuals to be discussed in one article, but we discuss only one from each study listed in Table 1.

### Berrebi and Klor 2008; a one-unit shift in X

"We find that the occurrence of a terror fatality within three months of the elections is associated with a .45 percentage point increase in the locality's relative electoral support for the right bloc of political parties, " (287).

# Gasper and Reeves; a one-unit shift in X

"Column 3 of Table 1 shows that a turn down is worth 2.7 points for an incumbent governor's vote share," (350).

# Ichino and Nathan 2009; a one standard deviation shift in X

"...a one standard deviation increase in the spatially weighted population share of Akans beyond a polling station (about 0.21) results in a predicted 6.9 percentage point greater NPP presidential vote share (95% CI: [5.7, 10.6])," (351-352).

## Scheve and Stasavage 2012; a one-unit/min. to max. shift in X

"... a country which mobilized for mass warfare for an entire five-year period increased its top inheritance tax rate by 18 to 23 percentage points compared to a country that did not mobilize for war," (94).

# Snyder and Strömberg 2010; a one-unit/min. to max. shift in X

"... a change from the lowest to the highest values of congruence is associated with a 28 percent increase in the probability of correctly recalling a candidate's name. This is about as large as the effect of changing a respondent's education from grade school to some college," (372).

# Fixed Effects Analysis in R

Jonathan Mummolo and Erik Peterson

The following code implements our recommendations for analyzing and interpreting fixed effects regression models. We will use Snyder and Strömberg (2010), discussed in the main text, as a working example.

### 1. Isolate Relevant Variation

First set your working directory and load the data.

```
##Set Working Directory here using setwd()
load("ss2.Rdata")
##rename dataframe
d<-congrecall</pre>
```

The following code replicates the second model in Table 4, Column 1 in Snyder and Strömberg (2010). The outcome is an indicator for whether an individual recalled their congressional representative's name, and the treatment, "cov2c," is media market congruence (range 0 to 1, continuous). The reported coefficient on the treatment in the published article is 0.28.

```
##estimate model of Name Recall with year and incumbent fixed effects
reg<-lm(cong_recall ~ cov2c + factor(year) + factor(incnum), data=d)
##view first two coefficients
summary(reg)$coefficients[1:2,]</pre>
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.03346182 0.10520300 0.318069 7.504376e-01
## cov2c 0.27878620 0.05459314 5.106616 3.325184e-07
##store estimation data
est<-reg$model
##make an object that is the variable name of the treatment
x<-"cov2c"
##store the coefficient estimate
b<-reg$coefficients[x]</pre>
```

We have replicated the result. Let's isolate the variation in the treatment being used to estimate this coefficient by residualizing the treatment with respect to the fixed effects.

x.resid<-lm(cov2c~factor(year) + factor(incnum), data=d)\$residuals</pre>

If this is the same variation being used to estimate the coefficient of interest, then we should be able to regress the outcome on this transformed treatment and get the same coefficient.

```
reg2<-lm(est$cong_recall ~x.resid)
summary(reg2)$coefficients[1:2,]</pre>
```

## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.3139543 0.003900063 80.499813 0.00000e+00
## x.resid 0.2787862 0.057599513 4.840079 1.311586e-06

We indeed get the same result. Note that we did not residualize the outcome, but if we did, we would also get the same coefficient on the treatment.

```
y.resid<-lm(cong_recall ~factor(year)+factor(incnum), data=d)$residuals
reg3<-lm(y.resid~x.resid)
summary(reg3)$coefficients[1:2,]</pre>
```

##EstimateStd. Errort valuePr(>|t|)## (Intercept)5.870861e-170.0035836511.638235e-141.000000e+00## x.resid2.787862e-010.0529264675.267425e+001.403801e-07

## 2. Identify a Plausible Shift in X

Now that we have isolated the relevant variation in the treatment and estimated the coefficient of interest, we need to determine what number to multiply the coefficient by to judge whether the treatment effect is substantively significant. The coefficient itself represents the effect of a one-unit shift in the treatment, which in this case is a shift from the theoretical minimum to the theoretical maximum of the variable. Is this a plausible shift?

```
range(est[,x])
```

```
## [1] 0.01890017 0.96752632
sdx<-sd(est[,x])
sdx
## [1] 0.2860724
sdxresid<-sd(x.resid)
sdxresid
## [1] 0.06771239
sdx/sdxresid
## [1] 4.224816
##compute % difference</pre>
```

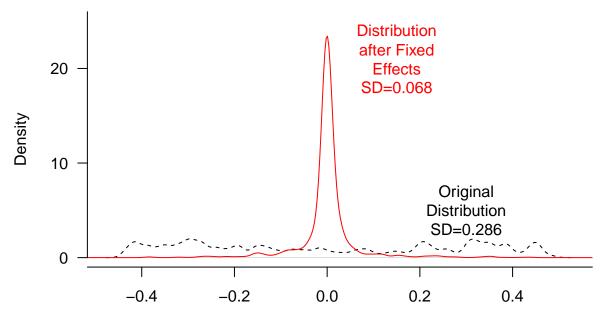
```
((sdxresid-sdx)/sdx)*100
```

### ## [1] -76.33033

From this basic analysis we learn that a 0-to-1 shift is beyond the observed range of the data [.019, .968]. Further, while the standard deviation of the original treatment is 0.29, the standard deviation of the transformed treatment used during estimation is 0.068, a reduction of 76%.

Let's visualize this reduction in variance. Overlapping density plots are useful for this. We will also center both variables on zero by demeaning them to make for an easier comparison of their spreads.

# **Treatment Distribution**



Treatment (Centered on Zero)

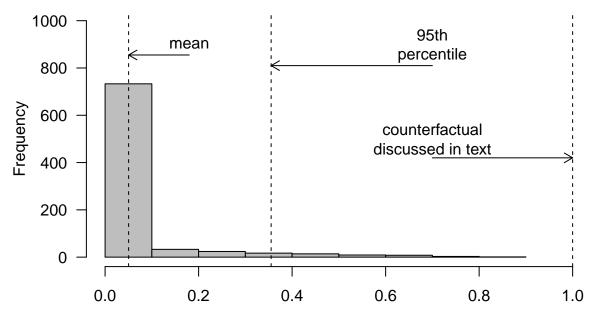
The plot makes very clear that a drastic reduction in variation has occurred as a result of the fixed effects being employed.

It is also useful to examine the distribution of within-unit ranges when trying to identify plausible counterfactuals. Let's generate that distribution and plot it as well. (Note: By not simultaneously accounting for the year and incumbent fixed effects, the variation plotted in the histogram below deviates slightly from the variation used to estimate the model, but is included to help motivate unit-based counterfactuals.)

```
bounds<-list(NA)</pre>
ranges<-NA
units<-unique(est[,"factor(incnum)"])</pre>
for(i in 1:length(units)){
  bounds[[i]]<-range(est[est[,"factor(incnum)"]==units[i],"cov2c"])</pre>
  ranges[i] <- bounds[[i]][2] - bounds[[i]][1]</pre>
}
hist(ranges, col="grey",
     main="Within-Unit Ranges\nof Treatment",
     xlab="Within-Incumbent Ranges", ylim=c(0,1000),xlim=c(0,1),axes=F)
axis(1, seq(0,1, by=.2))
axis(2, seq(0,1000, by=200), las=2)
abline(v=mean(ranges), lty=2)
abline(v=quantile(ranges, probs=.95), lty=2)
abline(v=1, lty=2)
text(x=.18,y=900,labels="mean")
```

```
text(x=.7,y=900,labels="95th\npercentile")
text(x=.7,y=500,labels="counterfactual\ndiscussed in text")
arrows(x0=.7,x1=1, y0=420, y1=420, length=.1)
arrows(x0=.18,x1=mean(ranges), y0=855, y1=855, length=.1)
arrows(x0=.7,x1=quantile(ranges, probs=.95), y0=810, y1=810, length=.1)
```

# Within–Unit Ranges of Treatment



## Within-Incumbent Ranges

As the histogram shows, the range of the treatment in the bulk of units is concentrated near zero, with a mean of roughly 0.05 and a 95th percentile of about 0.36.

With the above quantities in hand, researchers can now decide which counterfactual shift in the treatment they would like to discuss. They can also provide a sense of the plausibility of that counterfactual shift by describing where in the within-unit distribution the chosen shift is located.

```
##A within-unit SD shift
b*sdxresid

## cov2c
## 0.01887728
##A shift the size of the mean within-unit range
b*mean(ranges)

## cov2c
## 0.01402789
##A shift the size of the 95th percentile in within-unit ranges
b*quantile(ranges, probs=.95)
## cov2c
## 0.09900021
```

```
## A shift the size of the maximum within-unit range
b*max(ranges)
## cov2c
```

## 0.2272416
##How many ranges are zero?
mean(I(ranges==0))

## [1] 0.4429929

In addition, we learn that 44% of the within-unit ranges are zero.

##References Snyder, James M. and David Strömberg. 2010. "Press Coverage and Political Accountability." Journal of Political Economy, 118(2), 355-408.