# Administrative Records Mask Racially Biased Policing

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<sup>&</sup>lt;sup>1</sup>We thank Michael Pomirchy for research assistance.

# How do we measure racial bias in policing?



#### Eric Garner, 2014

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Sample selection bias due to post-treatment conditioning

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- Comparing white bank robbers to black civilians committing no crime. If we then found no disparity in rates of force against black/white civilians, that should be alarming!
- Current literature reads this result as "no evidence of racial bias in the use of force"

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- 6. New research designs to avoid this pitfall

# Defining the Statistical Problem

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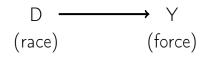
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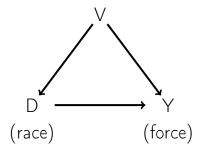
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- ▶ Racial bias in police stops (D<sub>i</sub> → M<sub>i</sub>) (e.g. Gelman, Fagan & Kiss 2007; Glaser 2014; Lerman & Weaver 2014; Goel, Rao & Shroff 2016)

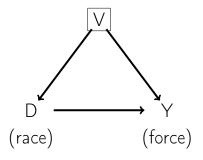
### Existing theory of race and police-civilian encounters



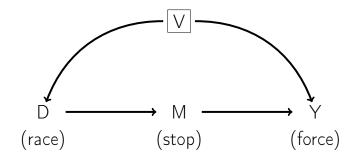
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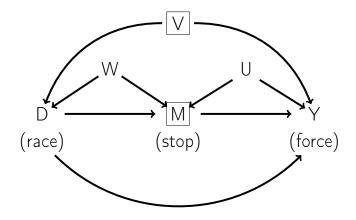
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# Formalizing the Missing Data Problem

## Solution: principal stratification

	$M_i(0)=1$	$M_i(0) = 0$
$M_i(1)=1$		
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What do we get to see in police data?

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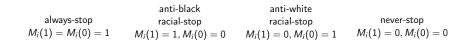
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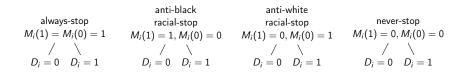
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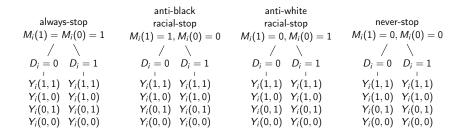
## Encounters (sightings) belong to one of four principal strata



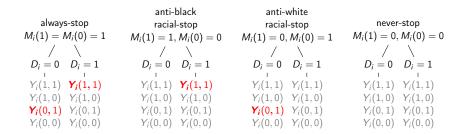
### Within each, civilian is treated (black) or not (white)



#### Four potential outcomes we may need to estimate



#### Very few potential outcomes appear in police data



## Causal Quantities of Interest

Prior work does not name specific causal estimands

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  - Average Treatment Effect (ATE) in the population
  - Effect among those who interact with police  $(ATE_{M=1})$
  - Effect among minorities who interact with police  $(ATT_{M=1})$

## Causal estimands

i	Stratum	Di	Mi	$M_i(0)$	$M_i(1)$	$Y_{i}(1,1)$	$Y_{i}(1,0)$	$Y_{i}(0,1)$	$Y_i(0, 0)$	ATE	$ATE_{M=1}$	$ATT_{M=1}$	$CDE_{M=1}$
1	Always-Stop	1	1	1	1	1	0	1	0	0	0	0	0
2	Always-Stop	0	1	1	1	1	0	1	0	0	0		0
3	Racial Stop	1	1	0	1	1	0	1	0	1	1	1	0
4	Never-Stop	0	0	0	0	1	0	0	0	0			

## Average Treatment Effect

$$ATE = \mathbb{E}[Y_i(1, M_i(1)) - Y_i(0, M_i(0))]$$

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## Average Treatment Effect Among the Stopped

 $ATE_{M=1} = \mathbb{E}[Y_i(1, M_i(1)) - Y_i(0, M_i(0))|M_i = 1]$ 

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Average Treatment Effect Among the Treated and Stopped

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- ▶ Goal: minimal, non-parametric, plausible

## Assumptions

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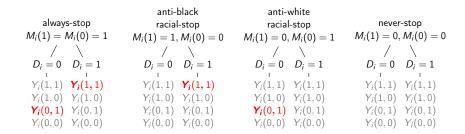
▶ If encounter not in the data, no force was applied

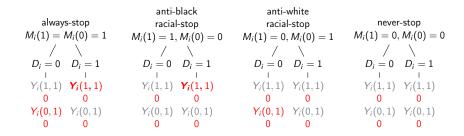
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- If encounter not in the data, no force was applied
- ► Highly plausible for lethal/severe force
- Increasingly plausible for sub-lethal force given civilian oversight boards, cell phone cameras



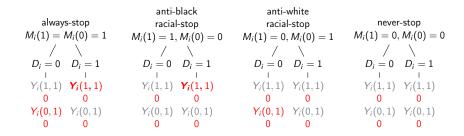


Assumption 2: Mediator monotonicity

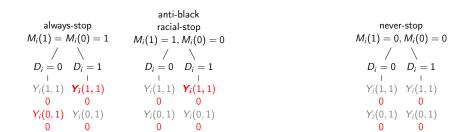
 $M_i(1) \geq M_i(0)$ 

## No anti-white bias in stopping

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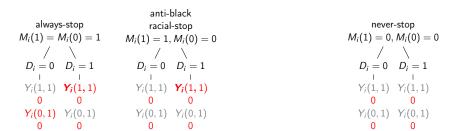


Assumption 3: Relative non-severity of racial stops

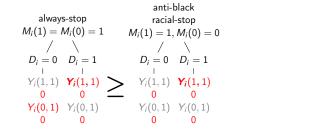
$$egin{aligned} & E[Y_i(d,m)|D_i=d',M_i(1)=1,M_i(0)=1] \geq \ & \mathbb{E}[Y_i(d,m)|D_i=d',M_i(1)=1,M_i(0)=0] \end{aligned}$$

Level of force applied in always-stop encounters (serious crimes) ≥ level applied in racial stop encounters on average

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$$\begin{array}{c} \text{never-stop} \\ \text{never-stop} \\ M_i(1) = 0, M_i(0) = 0 \\ / \\ D_i = 0 \\ D_i = 1 \\ I \\ Y_i(1, 1) \\ Y_i(1, 1) \\ 0 \\ Y_i(0, 1) \\ Y_i(0, 1) \\ 0 \\ 0 \end{array}$$

#### Assumption 4: Treatment ignorability

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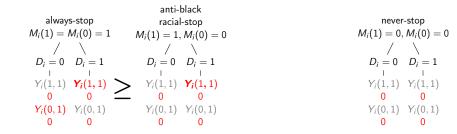
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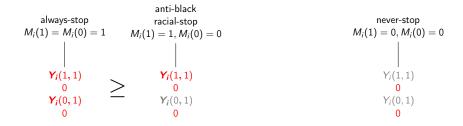
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- No omitted variables with respect to mediator or outcome
- More plausible in recent years (data on lat/lon, time, officer and suspect features, etc.)

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Given assumptions 1-4, can we recover a causal quantity?

Consider the naïve estimator:

$$\hat{\Delta} = \hat{\mathbb{E}}[Y_i | D_i = 1, M_i = 1] - \hat{\mathbb{E}}[Y_i | D_i = 0, M_i = 1]$$

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Biased even without omitted variables. Bias is always nonpositive.

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$$\begin{split} \mathbb{E}[\hat{\Delta}] - ATE_{M=1} \\ &= \left( \mathbb{E}[Y_i(1,1) - Y_i(0,1) | M_i(1) = 1, M_i(0) = 1] \right. \\ &- \mathbb{E}[Y_i(1,1) - Y_i(0,0) | M_i(1) = 1, M_i(0) = 0] \\ &\left. \right) \frac{\Pr(M_i(0) = 0 | D_i = 1, M_i = 1) \Pr(D_i = 1 | M_i = 1)}{- \left( \mathbb{E}[Y_i(1,1) | M_i(1) = 1, M_i(0) = 1] \right. \\ &- \mathbb{E}[Y_i(1,1) | M_i(1) = 1, M_i(0) = 0] \\ &\left. \right) \frac{\Pr(M_i(0) = 0 | D_i = 1, M_i = 1)}{- \mathbb{E}[Y_i(0,1) | M_i(1) = 1, M_i = 1)} \end{split}$$

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Biased even if goal is to estimate effect among the stopped. • More

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Can we estimate racial bias with police administrative data?

#### Bounds and bias correction

 Using precise form of bias, we can construct nonparametric sharp bounds on true effects

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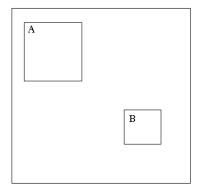
We don't, but we can place Fréchet bounds on Pr(A, B)

### Maurice Fréchet



Given two marginal distributions Pr(A) and Pr(B), the joint distribution Pr(A, B) is bounded by:

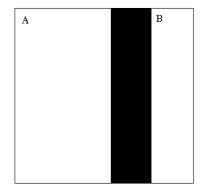
Given two marginal distributions Pr(A) and Pr(B), the joint distribution (A, B) is bounded by:



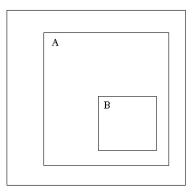
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А	В

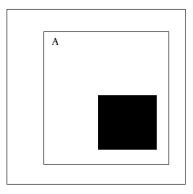
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- ▶ If we can bound Pr(A, B) we can also bound  $\theta = \frac{Pr(A, B)}{\rho}$  and plug the bounds back into the bias term
- If  $ATE_{M=1} = \mathbb{E}[\hat{\Delta}] + bias$ , then subbing in Fréchet bounds for  $\theta$  into the bias term  $\Longrightarrow$

$$\mathbb{E}[\hat{\Delta}] + \underline{\textit{bias}}_{LB} \le ATE_{M=1} \le \mathbb{E}[\hat{\Delta}] + \overline{\textit{bias}}^{UB}$$

### Sharp nonparametric bounds

Given  $\rho$ , bounds for the true  $ATE_{M=1}$  are given by:

$$\begin{split} \mathbb{E}[\hat{\Delta}] + \rho \ \mathbb{E}[Y_i | D_i = 0, M_i = 1] \ (1 - \Pr(D_i = 0 | M_i = 1)) \\ &\leq ATE_{M=1} \leq \\ \mathbb{E}[\hat{\Delta}] + \frac{\rho}{1 - \rho} \left( \mathbb{E}[Y_i | D_i = 1, M_i = 1] - K \right) \Pr(D_i = 0 | M_i = 1) \\ &+ \rho \ \mathbb{E}[Y_i | D_i = 0, M_i = 1] \ (1 - \Pr(D_i = 0 | M_i = 1)). \end{split}$$

where

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$$\mathcal{K} = \max\left\{0, 1 + \frac{1}{\rho}\mathbb{E}[Y_i|D_i = 1, M_i = 1] - \frac{1}{\rho}\right\}.$$

The  $ATT_{M=1}$  must similarly satisfy:

$$ATT_{M=1} = \mathbb{E}[\hat{\Delta}] + 
ho \ \mathbb{E}[Y_i | D_i = 0, M_i = 1]$$

Does this matter in practice?

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# Replication and Extension: Fryer (2019)

 Police-civilian interactions (e.g. Stop and Frisk, arrest records, summaries of shootings)

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Problem: No data on those police observe but do not stop

#### Concern over post-treatment bias

VOL. 2 NO. ISSUE

RACIAL DIFFER

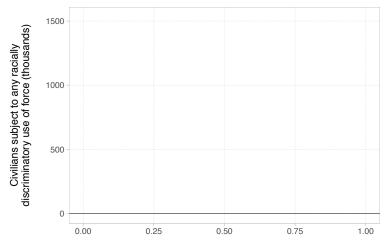
encounter recounted by police. A second type of bias is that officers may be more likely to charge black suspects with crimes such as resisting arrest or attempted assault on a public safety officer rather than misdemeanors, relative to whites, for identical behavior. This type of bias is an important limitation of Fryer (*forthcoming*) because it implies that the counterfactuals coded from arrest data may themselves contain bias. It is unclear how to estimate the extent of such bias or how to address it statistically.

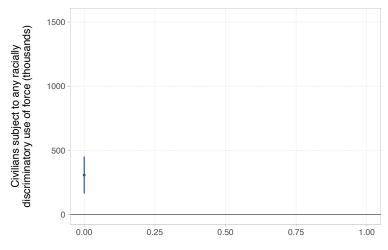
▶ Replicate two analyses of sub-lethal force using NYPD's "Stop, Question and Frisk" (SQF) data (2003-2013),  $N \approx 5$  million

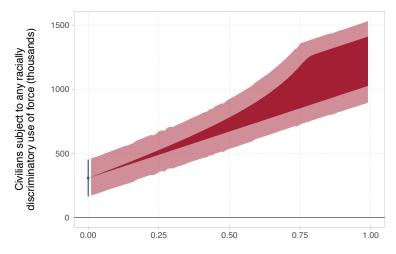
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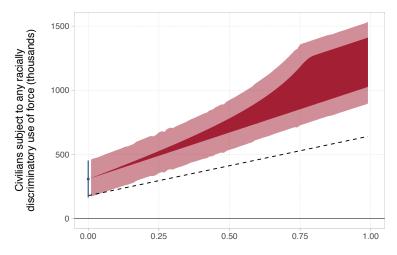
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  - Force thresholds (e.g. at least handcuffs) with seven categories: laying hands; push to wall; handcuffs; draw weapon; push to ground; point weapon; baton/pepper spray









What is the share of minority stops that would not have happened if civilians had been white?

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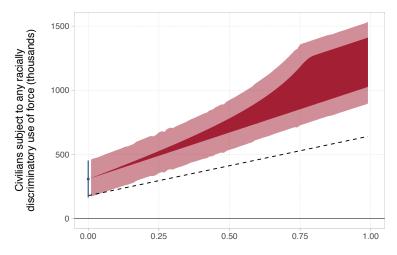
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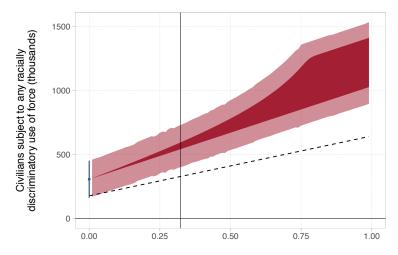
• We use 
$$\rho = .32$$
 to be conservative

# Bounds on race effects, black vs. white



Proportion of racially discriminatory stops

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Proportion of racially discriminatory stops

Minimum force	TE <sub>s</sub> for encounters with b No covariates		lack civilians (vs. white) Full specification	
	bounds	naïve	bounds	naïve
Use of hands	(112.66, 124.59)	61.69	(86.99, 96.74)	23.53
	(84.6, 151.84)	(32.89, 90.63)	(81.7, 102.15)	(16.41, 30.61)
Push to wall	(24.15, 27.75)	4.2	(26.48, 30.21)	6.67
	(15.5, 37.35)	(-5.29, 14.02)	(24.29, 32.38)	(3.73, 9.52)
Use of handcuffs	(14.6, 16.92)	1.32	(16.56, 19.02)	3.9
	(9.45, 22.61)	(-4.83, 7.53)	(15.05, 20.55)	(1.87, 5.88)
Draw weapon	(4.52, 5.14)	1.26	(4.71, 5.35)	1.46
	(3.13, 6.67)	(-0.33, 2.83)	(4.22, 5.86)	(0.79, 2.13)
Push to ground	(4.04, 4.58)	1.22	(4.11, 4.66)	1.26
	(2.79, 5.97)	(-0.21, 2.66)	(3.68, 5.09)	(0.68, 1.82)
Point weapon	(1.49, 1.7)	0.36	(1.64, 1.86)	0.55
	(0.96, 2.29)	(-0.29, 1)	(1.37, 2.13)	(0.18, 0.91)
Baton or pepper spray	(0.17, 0.19)	0.08	(0.17, 0.19)	0.07
	(0.1, 0.26)	(-0.01, 0.15)	(0.12, 0.24)	(-0.01, 0.14)

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# How can we do better?



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Only partially identified. Can't get the population ATE.

#### How can we do better?

- Only partially identified. Can't get the population ATE.
- Only way to do better: improved research design

# Option 1:

Identify situations with race-blind contact with police (e.g. rules for DUI stops; traffic stops and night; traffic accidents?)

Need data on those police observe but do not stop

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 Passive data collection on non-stop encounters.

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 Passive data collection on non-stop encounters.

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- Still have to contend with omitted variables
- But, plausible to measure most (all?) observable covariates available to officer when making stop

No need to condition on being stopped during analysis

Need data on those police observe but do not stop

Answer: traffic cameras.
 Passive data collection on non-stop encounters.

- Link cars to DMV records, ticket/arrest data
- Still have to contend with omitted variables
- But, plausible to measure most (all?) observable covariates available to officer when making stop
- No need to condition on being stopped during analysis
- Post-treatment conditioning avoided by design

Police data mask racially biased policing

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## Police data mask racially biased policing

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# Police data mask racially biased policing

- ► Lots of new/big data on policing → raft of studies estimating racial bias
- At present, inadequate theory: insufficient attention to role of race throughout entire process risks severely understating racial violence
- Risk confusing/misleading the public and policymakers

# Thanks!

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